



# Fractional derivative-based tracer analysis method for the characterization of mass transport in fractured geothermal reservoirs

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## ARTICLE INFO

### Article history:

Received 29 April 2013

Accepted 9 May 2014

Available online 12 June 2014

### Keywords:

Fractional advection-dispersion

Fractal geometry

Mass transport

Fractured reservoir

Geothermal resources

Reinjection

## ABSTRACT

The fractional advection-dispersion equation (fADE) has been proposed to describe mass transport in fractured reservoirs. This study develops a finite discrete method to solve the fADE and tests its accuracy against analytical solutions. Tracer simulation uses a three-dimensional simulation of flow analysis (FRACSIM-3D). The solution to the fADE incorporating a spatial fractional derivative shows reasonable agreement with the tracer response from FRACSIM-3D, which shows highly anomalous behaviors such as a long tail. The prediction by the fADE model is reasonably similar to those of FRACSIM-3D irrespective of differing well intervals.

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## 1. Introduction

The lifespan of geothermal resources may be prolonged by a reinjection process, thereby delaying pressure decline and preventing run-out of water in a geothermal reservoir (Stefansson, 1997; Kaya et al., 2011; Axelsson et al., 2005). However, one of the important problems with reinjection is the possibility of an early thermal breakthrough in production wells. Premature breakthrough and injection-induced cooling continue to be problems associated with injection into the geothermal reservoir. Evaluation of the effect of injected water on flow and thermal properties within the geothermal reservoir is essential for the optimal management and protection of subsurface fluid resources.

Tracer testing is a standard method of determining mass transport within a geothermal reservoir and can be a valuable tool in the design and management of production and injection operations (Horne, 1985; Niibori et al., 1995; Pruess, 2002). Methods

have also been discussed for predicting thermal breakthrough in fractured reservoirs based on information from tracer tests, e.g., Lauwerier (1955), Gringarten et al. (1975), Gringarten and Sauter (1975), Pruess and Bodvarsson (1984), and Kocabas (2005). Shook (2001) discussed the potential application of tracer data to provide relatively simple reservoir properties and to predict thermal breakthrough. Such information could provide a means of optimizing injection conditions and managing energy extraction (Wu et al., 2008). Furthermore, Lovekin and Horne (1989) and Juliusson and Horne (2013) reported methods for optimizing injection scheduling in geothermal reservoirs based on tracer return data using numerical simulations. In these cases, the production and injection wells were supposed to be already installed. The proposed method could be advantageous to predict mass transport at a location without any wells; and, based on field tracer data obtained from a limited number of wells, to determine where to optimally locate injection and/or production wells.

The inter-well properties provided by tracer tests are strongly controlled by the fracture geometries. Flow simulation models based on geological observation are often used to attempt quantitative assessment of tracer response curves. Discrete and continuous approaches form the two main branches in modeling the fluid flow and solute transport in fractured rocks. Simulations using the d

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